This policy is in line with the Mathematics National Curriculum 2014

Progression in written calculations Policy

Written October 2016 Nichola Martin This policy has been written in order to link to the National Curriculum introduced in September 2014, and aims to ensure consistency in the mathematical written methods and approaches to calculations across years 1-6. Reception needs will be addressed through Development Matters and Early Learning Goals.

The document is organised according to age related expectations, however it may be necessary for teachers to review lower year groups' expectations, in order to meet the needs of children working at a lower level.

The National Curriculum 2014 does not feature Using and Applying Maths separately, and so wherever possible, it is important for teachers to create real life contexts for learning in Maths.

As part of a child's learning in number calculation, they need to be taught how to select the best method according to the numbers. The hierarchy of thinking should be:



<u>Key Stage 1</u>

Children in Years 1 and 2 will be given a solid foundation in the basic building blocks of mental and written arithmetic. Through the teaching of place value, they will develop an understanding of how numbers work, so that they are confident with 2-digitnumbers and beginning to read and say numbers above 100.

A focus on number bonds, embedded through practical hands-on experiences, enables children to become secure with their knowledge of pairs of numbers to 10. They will then progress to pairs of numbers to 20. Their knowledge of number facts enables them to add several single-digit numbers, and to add/subtract a single digit number to/from a 2-digit number. Another important conceptual tool is the ability to add/subtract 1 or 10, and to understand which digit changes and why. This understanding is extended to enable children to add and subtract multiples of ten to and from any 2-digit number. The most important application of this knowledge is their ability to add or subtract any pair of 2-digit numbers by counting on or back in tens and ones. Children may extend this to adding by partitioning numbers into tens and ones. They will be taught to count in 2s, 3s. 5s and 10s, and will have related this skill to repeated addition. They will have met and begun to learn the associated 2x, 3x, 5x and 10x tables. Engaging in a practical way with the concept of repeated addition and the use of arrays enables children to develop a preliminary understanding of multiplication, and asking them to consider how many groups of a given total will introduce them to the idea of division. They will also be taught to double and halve numbers, and will thus experience scaling up or down as a further aspect of multiplication and division.

Key Stage 2

In Years 3 and 4 build on the concrete and conceptual understandings they have gained in KS1 to develop a real mathematical understanding of the four operation, in particular developing arithmetical competence in relation to larger numbers. In addition and subtraction, they are taught to use place value and number facts to add and subtract numbers mentally and will develop a range of strategies to enable them to discard the 'counting in ones' or fingers-based methods of the infants. In particular, they will learn to add and subtract multiples and near multiples of 10, 100 and 1000, and will become fluent in complementary addition as an accurate means of achieving fast and accurate answers to 3-digit subtractions. Standard written methods for adding larger numbers are taught, learned and consolidated, and written column subtraction is also introduced. This key stage is also the period during which all the multiplication and division facts are thoroughly memorised, including all facts up to the 12 x 12 table. Efficient written methods for multiplying or dividing a 2-digit or 3-digit number by as single-digit number are taught, as are mental strategies for multiplication or division with large but friendly numbers, e.g. when dividing by 5 or multiplying by 20. Children will develop their understanding of fractions, learning to reduce a fraction to its simplest form as well as finding non-unit fractions of amounts and quantities. The concept of a decimal number is introduced and children consolidate a firm understanding of one-place decimals, multiplying and dividing whole numbers by 10 and 100.

In Years 5 and 6, children move from dealing mainly with whole numbers to performing arithmetic operations with both decimals and fractions. They will consolidate their use of written procedures in adding and subtracting whole numbers with up to 6 digits and also decimal numbers with up to two decimal places. Mental strategies for adding and subtracting increasingly large numbers will also be taught. These will draw upon children's robust understanding of place value and knowledge of number facts. Efficient and flexible strategies for mental multiplication and division are taught and practiced, so that children can perform appropriate calculations even when the numbers are large, such as $40,000 \times 6$ or $40,000 \div 8$. In addition, it is in Y5 and Y6 that children extend their knowledge and confidence in using written algorithms for multiplication and division. Fractions and decimals are also added, subtracted, divided and multiplied, within the bounds of children's understanding of these more complicated numbers, and they will also calculate simple percentages and ratios. Negative numbers will be added and subtracted.

Year 1 Add with numbers up to 20

Use numbered numberlines to add, by counting on in ones, encouraging children to begin with larger number and then count on.



Children should:

- have access to a range of equipment eg. number lines, counting apparatus, Numicon, 100 squares, bead strings etc.
- be shown numbers in a range of contexts
- read and write number sentences using the = and
 + signs
- interpret number sentences including missing number problems eg. 3 + ? = 8.

<u>Key vocabulary</u> add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line

Key Skills for addition at Year 1

- Read and write numbers to 100 in numerals (1-20 in words)
- Count to and across 100

Z

- Recall bonds to 10 and 20, and addition facts within 20 ('story of' 5, 6, 7, 8, 9 and 10)
- Count on in ones from a given 2-digit number
- Add two single-digit numbers by counting on
- Add three single-digit numbers spotting doubles or pairs to 10
- Count on in tens from any given 2-digit number
- Add 10 to any given 2-digit number
- Use number facts to add single-digit numbers to two-digit numbers, e.g. use 4 + 3 to work out 24 + 3, 34 + 3...
- Add by putting the larger number first
- Recognise doubles to double 6

Year 2 Add with 2-digit numbers (develop mental fluency with place value and addition using 2-digit numbers, then move to formal methods)

Add 2-digit numbers and tens, 2-digit numbers and units, two 2-digit numbers, first practically using equipment (eq. Numicon, Dienes, 100 squares) then using empty number line.

Children move to more formal recording methods using

20+5 40+7 20 + 40 = 605+7 = 12

partitioning methods:

This may need to be modelled practically using apparatus such as Dienes or Numicon:



Key vocabulary add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary

Key Skills for addition at Year 2

Z

- Locate any 2-digit number on a landmarked line and use this to compare numbers; record comparisons < and >, e.g. 56 > 39.
- Identify any number on the 1-100 number grid; understand that each number is a multiple of ten and some ones, e.g. 54 is 50 and 4 more.
- Add two single digit numbers (8 + 7) by counting up; add two 2-digit numbers which total less than 100 by counting on in tens and ones, e.g. 54 + 37 as 54 + 30 + 7.
- Know securely number pairs for all the numbers up to and including 12
- Count in steps of 2, 5, and 10 from 0.
- Know different unit patterns when not crossing a ten, e.g. 4 + 3 = 7, 14 + 3 = 17, 24 + 3 = 27
- Begin to recognise unit patterns when crossing a ten, e.g. 5 + 6 = 11
- Know pairs with a total of 20 and multiples of 10 to 100
- Count on in ones and tens from any given 2-digit number
- Add two or three single-digit numbers
- Add a single-digit number to any 2-digit number using number facts, including bridging multiples of 10. Add 10 and small multiples of 10 to any given 2-digit number
- Add any pair of 2-digit numbers
- Know that adding can be done in any order
- Solve problems with addition using concrete objects, pictorial representations, involving numbers, quantities and measures, applying written and mental methods

<u>Year 3</u> Add numbers up to 3 digits (use partitioning method for addition to add two or three 2-digit numbers or three 2-digit numbers. Begin to use column addition to add numbers with three digits)



Children who are very secure and confident with 3-digit expanded and column addition, should be moved onto the compact column addition method, involving carrying.

<u>Key vocabulary</u> add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary, hundreds boundary, increase, vertical, 'carry', expanded, compact

Key Skills for addition at Year 3

• Know pairs with each total to 20

Z

- Know pairs of multiples of 10 with a total of 100
- Add any two 2-digit numbers by counting on in 10s and 1s or by using partitioning
- Add multiples and near multiples of 10 and 100
- Add 1,10, 100 to 3-digit numbers
- Understand place value in 3-digit numbers
- Perform place value additions without a struggle. (E.g. 300 + 8 + 50 = 358)
- Use place value and number facts to add a 1-digit or 2-digit number to a 3-digit number number. (E.g. 104 + 56 is 160 since 104+50=154 and 6+4=10 and 676 + 8 is 684 since 8=4+4 and 76+4+4=84)
- Add pairs of 'friendly' 3-digit numbers mentally, e.g. 320 + 450
- Begin to add amounts of money using partitioning.
- Solve problems with addition using number facts, place value, missing numbers.



<u>Key vocabulary</u> add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary, hundreds boundary, increase, vertical, 'carry', expanded, compact, thousands, hundreds, digits, inverse

Key Skills for addition at Year 4

- Select appropriate method, mental, jottings, written—and explain why
- Add any two 2-digit numbers by partitioning or counting on
- Know by heart/quickly derive number bonds to 100 (eg 32 + 68) and to £1 (64p + 36p)
- Add to the next hundred, pound and whole number. (E.g. 234 + 66 = 300, 3.4 + 0.6 = 4)
- Perform place value additions without a struggle. (E.g. 300 + 8 + 50 + 4000 = 4358)
- Add multiples and near multiples of 10, 100 and 1000.
- Add £1, 10p, 1p to amounts of money
- Use place value and number facts to add 1-, 2-, 3-and 4-digit numbers where a mental calculation is appropriate'. (E.g. 4004 + 156 by knowing that 6+4=10 and that 4004+150= 4154 so total is 4160)
- Perform inverse operations to check
- Solve 2-step problems in context
- Continue to practise a wide range of mental addition strategies eg. Round and adjust, near doubles, numbers bonds, partitioning and recombining



<u>Key vocabulary</u> add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary, hundreds boundary, increase, vertical, 'carry', expanded, compact, thousands, hundreds, digits, inverse, decimal places, decimal point, tenths, hundredths, thousandths.

Key Skills for addition at Year 5

- Locate 5 and 6 digit numbers on a landmarked line; use this to compare/order numbers.
- Round to ten, a hundred, a thousand or ten thousand.
- Use rounding to check accuracy
- Understand a one-place decimal number as a number of tenths and a two-place decimal number as a number of hundredths.
- Add or subtract 0.1 or 0.01 to/from any decimal number with confidence, e.g. 5.83 + 0.01 or 4.83 - 0.1
- Add and subtract mentally with confidence where the numbers are less than 100 or the calculation relies upon simple addition and place value.
- Confidently add numbers with more than 4-digits using a secure written method, including adding 'piles' of numbers
- Use inverse to check calculations

<u>Year 6</u> Add several numbers of increasing complexity including money, measures and decimals with different numbers of decimal places.

Tenths, hundredths and thousandths should be correctly aligned, with the decimal point aligned vertically, including in the answer.

> Empty decimal places can be filled to with zero to show the place value of each column

Use compact column method to add in context of money, measures, including decimals with different numbers of decimal places.

Pupils should apply their knowledge of a range of mental strategies, mental recall skills, informal and formal written methods when selecting the **appropriate method** to work out addition problems. Opportunities to discuss the appropriateness of methods need to be planned for.



<u>Key vocabulary</u> add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary, hundreds boundary, increase, vertical, 'carry', expanded, compact, thousands, hundreds, digits, inverse, decimal places, decimal point, tenths, hundredths, thousandths.

Key Skills for addition at Year 6

- Add mentally with confidence using larger numbers and calculations of increasing complexity
- Add several large numbers using written addition
- Add several large or decimal numbers using written addition
- Perform mental calculations, including with mixed operations and large numbers, using a range of strategies
- Solve multi-step problems
- Use estimation and inverse to check the validity of an answer

ADDITION

Year 1 Subtract from numbers up to 20

Children consolidate understanding of subtraction practically using bead strings, cubes etc and in real life contexts. They are introduced to more formal recording using number lines, then using empty numbers lines.



Model subtraction practically and using number tracks, number lines and 100 squares

and practically. Find the difference between - this is to be done practically using

the language 'find the distance between' and 'how many more than?'

This will be introduced practically with the language 'find the	7	'Seven is 3 more than four'
distance between' and 'how many more?' in a	4	'I am 2 years older than my
range of familiar contexts.		sister'

<u>Key vocabulary</u> equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is ...

Key skills for subtraction at Year 1

- Give a number, say one less
- Count back in ones to/from 100 and from any single-digit or 2-digit number
- Count back in tens from any 2-digit number
- Locate any number on a 1-100 grid or a beaded line 0-100
- Know number bonds to 10, also know what is left if objects are taken from 10, eg. 10 fingers, fold down 4, leaves 6 standing
- Solve one-step problems involving subtraction, using concrete objects (bead strings, objects, cubes) and pictures, and missing number problems
- Recognise the and = signs, and use these to read and write simple subtractions

Year 2 Subtract with 2-digit numbers

Use practical equipment such as Dienes and Numicon to model subtraction.

Subtract first on a numbered number line, then on an empty number line, by counting back, aiming to develop mental subtraction skills.



Children should also learn how to count on in order to find the difference. They should be given opportunities to explore when to count on and when to count back.



<u>Key vocabulary</u> equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is ..., difference, count on, strategy, partition, tens, units

Key skills for subtraction at year 2

SUBTRACTION

- Recognise that addition and subtraction are inverse operations and understand that 10-4=6 as well as 6+4=10
- Count back in ones or tens to take away eg. 27-3= or 54-20 =
- Begin to count up to find a difference between two numbers with a small gap (42-38). Know when to count on and when to count back
- Recall and use subtraction facts to 20 fluently
- And derive and use related facts to 100
- Subtract using concrete objects, pictorial representations, 100 squares, Diennes/Numicon and mentally, including a 2-digit number and ones, a 2-digit number and tens and two 2-digit numbers
- Use inverse to check calculations



<u>Key vocabulary</u> equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is ..., difference, count on, strategy, partition, tens, units, take and make, exchange, digit, value, hundreds

Key skills for subtraction at Year 3

- Understand place value in 3-digit numbers; add and subtract 1s, 10s or 100s without difficulty; use this to add and subtract multiples of 1,10, 100 to/from 3-digit numbers
- Mentally subtract any pair of 2 digit numbers, eg. 75-58
- Recognise that there are two ways of completing subtractions, either by counting up (using empty number line) or by counting back, eg. 54-3 (counting up)
- Subtract mentally using place value and number bonds, eg. 347-5, 347-40, 347-100

Year 4 Subtract with up to 4-digit numbers Subtract using formal column subtraction, using take and make where appropriate.

Use complementary addition to subtract amounts of money, and for subtractions

where the larger number is a near multiple of 1000 or 100.

+102

1865 1870 1900 2002 Use counting up with confidence to solve most subtractions, including finding complements to multiples of 100 (Eg. 512
 - 287 is done by
 NB. Children should be encouraged to progress to using the fewest number of jumps.

<u>Key vocabulary</u> equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is ..., difference, count on, strategy, partition, tens, units, take and make, exchange, digit, value, hundreds, inverse

Key skills for subtraction at Year 4

+5

+30

- Mentally subtract any pair of two digit numbers
- Subtract 3 digit numbers from 3 digit numbers using counting on, eg. 426-278 by jumping along a line from 278 to 426
- Practise mental subtraction strategies eg. round and adjust (37-9) using place value
- Use counting on in the context of money and also when subtracting from numbers ending in zeros eg. 4000-372
- Count backwards through zero, using negative numbers



<u>Key vocabulary</u> equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is ..., difference, count on, strategy, partition, tens, units, take and make, exchange, digit, value, hundreds, inverse, tenths, hundredth, decimal point, decimal

Key skills for subtraction at Year 5

- Count backwards through zero, using negative numbers
- Add or subtract 0.1 or 0.01 to/from any decimal number with confidence, eg. 5.83 + 0.01 or 4.83 0.1
- Children need to utilise and consider a range of subtraction strategies, jottings and written methods before choosing how to calculate
- Subtract larger numbers using column subtraction or by counting up
- Begin to subtract decimal numbers using counting up: 6.2 3.5
- Decide which mental methods to use and explain why

 $\underline{Year \ 6}$ Subtracting with increasingly large and more complex numbers and

decimal values

including money, measure and decimals with different numbers of decimal places



Use the compact column method to subtract more complex integers.

	X	10	'5	3K	ų.	9	kg
-		3	6	0	8	0	kg
		6	9	3	3	9	kg

Empty decimal places should be filled with a zero to show the place value of each column.

Pupils should apply their knowledge of a range of mental strategies, mental recall skills, informal and formal written methods when selecting the appropriate method to work out subtraction problems. Opportunities to discuss the appropriateness of methods needs to be planned for.

<u>Key vocabulary</u> equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is..., difference, count on, strategy, partition, tens units, take and make, exchange, digit, value, hundreds, inverse, tenths, hundredths, decimal point, decimal

Key skills for subtraction at Year 6

- Subtract mentally with confidence where the numbers are less than 100 or the calculation relies upon simple subtraction and place value. Eg. 6,723 400, 72 45, 100 64
- Subtract large numbers using column subtraction or counting up, eg. 1,323 758
- Subtract decimal numbers in context and calculate intervals across zero
- Children need to utilize and consider a range of mental subtraction strategies, jottings and written methods before deciding how to calculate
- Decide which methods to use and explain why

<u>Year 1</u> Multiplly with concrete objects, arrays and pictorial representations



Count in 2s, 5s, 10s.

Use visual and concrete arrays and 'sets of' objects to find the answers to '3 lots of 4' or '2 lots of 5'

0000	0000

Find doubles to double 6 eg. with Numicon



Key vocabulary groups of, lots of, times, array, altogether, multiply, count

- Count in multiples of 2, 5 and 10
- Recognise doubles to double 6
- Solve simple one-step problems involving multiplication and division, calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher

<u>Year 2</u> Multiplication using arrays and repeated addition

(using at least 2s, 5s and 10s).

Starting from zero, make equal jumps on a number line to work out multiplication



facts and write multiplication facts.

Use arrays to help children to understand the commutative law of multiplication.



Learn doubles to double 20. Begin to double multiples of 5 to 100. Begin to double 2-digit numbers less than 50 with1s digit of 1, 2, 3, 4 or 5.

<u>Key vocabulary</u> groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, sets of, equal groups, times as big as, once, twice, three times ...

X

- Count in steps of 2, 3 and 5 from zero and in 10s from any number
- Know the 2x, 5x and 10x tables and begin to say how many 10s are in 40 or how many 5s are in 30; recognise odd and even answers
- Write and calculate number statements using x and = signs
- Show that multiplication can be done in any order
- Solve a range of problems involving multiplication, using concrete objects, arrays, repeated addition, Numicon, mental methods and multiplication facts

MULTIPLICATION

<u>Year 3 multiply 2-digit numbers by a single digit number</u>

Introduce the grid method for multiplying 2 digits by 1 digit

			(×1	10	1 4
x	20	3		00000000	000000
8	160	24		200000000000000000000000000000000000000	000000
			• Ŏ	50000000	500000

Demonstrate how the array links to the grid calculation.

Children MUST be able to do the following before moving on to the grid method:

- Partition numbers into tens and units
- Multiply multiples of ten by a single digit using their knowledge of multiplication facts and times tables Eg. 30 × 80 = 2400

Because 3x8=24

• Recall and work out multiplication facts in the 2, 3, 4, 5, 8 and 10 times tables.

<u>Key vocabulary</u> groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, sets of, equal groups, times as big as, once, twice, three times ..., partition, grid method, multiple, product, tens, units, value

- Understand that multiplication is commutative, eg. 4 \times 8 is the same as 8 \times 4
- Know the 2x, 3x, 5x and 10x tables. All tables need to be learned to the $12^{\,\rm th}$ multiple
- Multiply any 2-digit number by 10 or a single-digit number by 100
- Understand the effect of multiplying whole numbers by 10 and 100
- Multiply a 1-digit number by a 2-digit number starting to use the grid method
- Solve multiplication problems involving missing numbers

Year 4 Multiply 2 and 3 digit by a single digit

using all multiplication tables up to 12×12 .

Developing	the grid me	thod:		
Eq.	136 x <u>5</u> =	680		500
Jac Barrier	Subsection.			150
X	100	30	6	
5	500	150	30	+ 30
				680

Encourage mental addition or use column addition to add accurately.

Move onto short multiplication (see Yr5) if and when the children are confident and accurate multiplying 2 and 3 digit numbers by a single digit this way and are already confident in carrying for written addition.

Children should be able to:

- Approximate before they calculate and make this a regular part of their calculating, going back to their approximation to consider the reasonableness of their answer
- Record an approximation to check their answer against
- Multiply multiples of 10 and 100 by a single digit
- Recall all times tables up to 12 x 12

<u>Key vocabulary</u> groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, sets of, equal groups, times as big as, once, twice, three times ..., partition, grid method, multiple, product, tens, units, value, inverse

Key skills for multiplication at Year 4

- Multiply 1 and 2 digit numbers by 10, 100 and 1000; to understand place value in decimal numbers with one place
- Know and recite all times tables up to 12th multiple; include multiplying by 0
- Multiply 1-digit numbers by 2-digit numbers or friendly 3-digit numbers using grid method
- Find doubles to double 100 and beyond, using partitioning
- Begin to double amounts of money
- Use doubling as strategy for multiplying by 2, 4, 8 and also 3, 6
- Count in multiples of 6, 7, 9, 25 and 1000

MULTIPLICATION

×

Year 5 Multiply up to 4 digits by 1 or 2 digits

MULTIPLICATION

introducing column multiplication.

Introduce column multiplication by comparing a grid method calculation, in order to see how the steps are related. Notice how there are less steps.



Introduce long multiplication for multiplying by 2 digits

Again this could be developed from the grid method.

×	300	40	3
20	6000	800	60
4	1200	160	12

6860 + 1372 = 8232

Move towards more complex numbers



Children should approximate



<u>Key vocabulary</u> groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, sets of, equal groups, times as big as, once, twice, three times ..., partition, grid method, multiple, product, tens, units, value, inverse, square, factor, integer, decimal, short/long multiplication, 'carry'

- Know and recite all times tables including division facts
- Multiply 2 and 3 digit numbers by numbers less than 12 using grid method; multiply 2-digit by 2-digit numbers using grid method
- + Identify multiples and factors, using knowledge of multiplication tables up to 12×12
- Scale up or down by a factor of 2, 5 or 10
- Multiply integers and decimals by 10, 100 or 1,000
- Recognise and use squares, cubes and their notations

MULTIPLICATION

<u>Year 6</u> Short and long multiplication, and multiply decimals with up to 2 places by a single digit number.

23.4
x <u>8</u>
18.72
23

8.72

Line up decimal point in guestion and answer.

Use this method for money and measures,

Children should:

- Use rounding and place value to make approximations before calculating and use these to check validity of answers
- Use short multiplication to multiply numbers with more than 4 digits by a single digit; to multiply money and measures; and to multiply decimals up to 2 decimal places by a single digit
- Use long multiplication to multiply numbers with at least 4 digits by a 2-digit number

<u>Key vocabulary</u> groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, sets of, equal groups, times as big as, once, twice, three times ..., partition, grid method, multiple, product, tens, units, value, inverse, square, factor, integer, decimal, short/long multiplication, 'carry', tenths, hundredths, decimal

- Recall multiplication facts up to 12x12
- Use short/long multiplication to multiply by 1 and 2-digit numbers
- Use short multiplication to x a 1-digit number by a decimal number
- Multiply fractions and mixed numbers by whole numbers
- Multiply fractions by proper fractions
- Estimate answers using rounding and approximation

Year 1 Group and share small quantities

Using both objects and pictorial representations to solve problems involving both grouping and sharing.

Children should solve a division problem within a context. Eg. 5 children share 15 sweets. How many does each child get?



Can they solve this and write a division statement eg. 15 sweets shared between 5 children gives us 3 each.

Pupils should:

- use lots of practical apparatus, arrays and picture representations
- Understand the difference between "grouping" objects (How many groups of 2 can you make?) and "sharing" (Share these sweets between 2 people)
- Be able to count in multiples of 2s, 5s and 10s
- Find half of a group of objects by sharing into 2 equal groups

<u>Key vocabulary</u> share, share equally, one each, two each..., group, groups of, lots of, array

- Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations, arrays with the support of the teacher
- Through grouping and sharing small quantities, pupils begin to understand division and finding simple fractions of objects, numbers and quantities
- They make connections between arrays, number patterns and counting in 2s, 5s and 10s.

<u>Year 2</u> Group and share using the \div and = signs

Use objects, Numicon, arrays, pictorial representation and grouping.



<u>Key vocabulary</u> share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over

- Count in steps of 2, 3 and 5 from 0
- Recall and use multiplication and division facts for the 2, 5 and 10xtables, including recognising odd and even numbers
- Calculate mathematical statements for x, ÷ and = signs
- Show that multiplication can be done in any order (commutative) and division of one number by another cannot
- Solve problems involving multiplication and division facts, including problems in contexts



<u>Key vocabulary</u> share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple

- Recall and use division facts for the 2, 3, 4, 5,8 and 10 multiplication tables
- Write and calculate mathematical statements for division using the x tables they know, including for 2-digit numbers divided by one digit
- Solve problems in contexts, and including missing number problems, involving division
- Develop efficient mental methods, eg. using division facts (eg. use 3x2=6, 6÷3=2 etc) to derive related facts (30x2=60, so 60÷3=20 etc)
- Develop reliable written methods for division, starting with calculations of 2-digit numbers by 1-digit numbers using a ENL
- Halve even numbers up to 50 and multiples of ten to 100
- Perform divisions within the tables including those with remainders, eg 38÷5

<u>Year 4</u> Divide up to 3-digit numbers by a single digit

Short division: limit numbers to NO remainders in the answer OR $\ensuremath{\mathsf{ca}}$

rried (each digit must be a multiple of the divisor).



Once children are secure with division as grouping, demonstrate this using number lines, arrays etc., short division for larger 2-digit number should be introduced, initially with carefully selected examples requiring no calculating of remainders at all.



Move to short division with remainders.



<u>Key vocabulary</u> share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple, divisible by, factor

- Use a written method to divide a 2-digit or 3-digit number by a single-digit number
- Give remainders as whole numbers
- Recall x and ÷ facts for all tables up to 12×12
- Use place value, known and derived facts to x and ÷ mentally
- Become fluent in the formal written method of short division with exact answers when dividing by a 1-digit number
- Practise mental methods and extend this to 3-digit numbers to derive facts eg.
 200x3=600 so 600÷3=200
- Solve two step problems in contexts, choosing appropriate operation

<u>Year 5</u> Divide up to 4 digits by a single digit \leq 12 including answers with remainders

Short division including remainder answers. Refer to Yr4 or Yr3 if necessary to ensure children are confident in the steps towards short division.



The answer could be expressed as 663 remainder 5 or as 663 and 5/8 or as a decimal. Division should be given in a real life context, including using money and measures so that pupils know to round up or down. Answers could be given as remainders, decimals or fractions.

Once children's understanding of this method is secure they might shorten their dialogue to: "How many 8s in 53?" "6 remainder 5" etc.

Ensure children have a secure understanding of what they are doing and are able to use their knowledge of related facts to either make a rough estimate first or have an idea about whether their final answer is reasonable or not.

<u>Key vocabulary</u> share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple, divisible by, factor, quotient, prime number, prime factors, composite number (non-prime)

Key skills for division at Year 5

Recall multiplication and division facts for all numbers up to 12x12

- Multiply and divide numbers mentally, drawing upon known facts
- Identify multiples and factors, including finding all factor pairs of a number, and common factors or two numbers
- Solve problems involving x and division where larger numbers are decomposed into their factors
- Multiply and divide whole numbers and those involving decimals by 10, 100 and 1000
- Use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers
- Work out whether a number up to 100 is prime, and recall prime numbers to 19
- Divide numbers up to 4-digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context
- Use multiplication and division as inverses. Interpret non-integer answers to division by expressing results indifferent ways according to the context, including with remainders, as fractions, as decimals or by rounding.

<u>Year 6</u> Divide at least 4-digit numbers by single and 2-digit numbers (including decimals)

Short division (for dividing by a single digit)

Children should continue to use short division with remainders. They need to know how to express an answer as a remainder, a fraction or as a decimal.

Introduce long division by chunking for dividing by 2-digits.



100x = 3600

Find out "how many 36s are in 972" by subtracting 'chunks' of 36 until zero is reached or until there is a remainder.

Teach pupils to write a 'useful list' first at the side that will help them decide what chunks to use.

Introduce simply by limiting choice of chunks to lots of 10 or 100. As children beome confident they can be encouraged to use more efficient chunks eg. 20x or 5x.

<u>Key vocabulary</u> share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple, divisible by, factor, quotient, prime number, prime factors, composite number (non-prime), common factor

- Recall and use x and ÷ facts for all numbers to 12x12 for more complex calculations
- Divide numbers up to 4-digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, decimals or by rounding as appropriate for the context. Use short division where appropriate
- Perform calculations including with mixed operations and large numbers
- Identify common factors, common multiples and prime numbers
- Solve problems involving all 4 operations
- Use estimation to check answers to calculations and determine accuracy in the context of a problem
- Use written division methods in cases where the answer has up to two decimal places
- Solve problems which require answers to be rounded to specified degrees of accuracy